

P180

1. Если $u = x^2/(x^2 + y^2)$,
найти $\partial u/\partial x, \partial u/\partial y$.

2. Если $s = t^u$, найти $\partial s/\partial t, \partial s/\partial u$.

3. Если $z = \ln \sqrt{u^2 + v^2 + w^2}$,
найти $\partial z/\partial u, \partial z/\partial v, \partial z/\partial w$.

4. Для $w = x^3 - y^3 - 2xy + 6$, найти $\partial^2 w/\partial x^2$ и $\partial^2 w/\partial y^2$
в точках, где $\partial w/\partial x = \partial w/\partial y = 0$.

5. Для $w = 8x^4 + y^4 - 2xy^2$, найти $\partial^2 w/\partial x^2$ и $\partial^2 w/\partial y^2$
в точках, где $\partial w/\partial x = \partial w/\partial y = 0$.

Если $z = x^2 + 2y^2, x = r \cos \theta, y = r \sin \theta$,
найти частные производные:

7. $\left(\frac{\partial z}{\partial x}\right)_y$ 8. $\left(\frac{\partial z}{\partial x}\right)_r$ 9. $\left(\frac{\partial z}{\partial x}\right)_\theta$ 10. $\left(\frac{\partial z}{\partial y}\right)_x$ 11. $\left(\frac{\partial z}{\partial y}\right)_r$ 12. $\left(\frac{\partial z}{\partial y}\right)_\theta$